# Concerning the Intersecting Tunnel Structure of a Novel Vanadyldiphosphate $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$ and Its Structural Relationships with Other V(V) and V(IV) Phosphates and Relatives 

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#### Abstract

$\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}, \mathrm{Mr}=626.91$, orthorhombic, Pna21, $a=17.407(1), b=11.3438(7), c=7.2964(15) \AA, V=$ $1440.8(5) \AA^{3}, Z=4, D_{x}=2.89 \mathrm{Mg} \mathrm{m}^{-3}, \lambda(\mathrm{MoK} \alpha)=0.71073 \AA, \mu(\mathrm{MoK} \alpha)=2.96 \mathrm{~mm}^{-1}, F(000)=1212$, $T=293 \mathrm{~K}, R=0.049$, and $R_{\mathrm{w}}=0.055$ for 574 independent observed reflections with $I \geq 3 \sigma(I)$. The host lattice $\left[\mathrm{V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}\right]$ is built up from corner-sharing $\mathrm{VO}_{6}$ octahedra, $\mathrm{VO}_{5}$ square pyramids, and $\mathrm{PO}_{4}$ tetrahedra. The structure can be described in terms of mixed chains [ $\left.\mathrm{V}_{2} \mathrm{P}_{8} \mathrm{O}_{30}\right]_{\infty}$ linked through $\left[\mathrm{V}_{2} \mathrm{O}_{10}\right.$ ] units. The $\left[\mathrm{V}_{2} \mathrm{P}_{8} \mathrm{O}_{30}\right]_{\infty}$ chains are formed of $\mathrm{ReO}_{3}$-type chains connected to diphosphate groups whereas the $\left[\mathrm{V}_{2} \mathrm{O}_{10}\right.$ ] units are formed from one corner-shared $\mathrm{VO}_{6}$ octahedron and one $\mathrm{VO}_{5}$ pyramid. The framework delimits intersecting tunnels running along $c$ and $b$ which suggest possible ion exchange properties. The ability of $\mathrm{V}(\mathrm{IV})$ to form a short vanadyl bond $\mathrm{VO}^{2+}$ is observed in all the vanadium polyhedra leading to the formula $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$. A comparison of the structure with that of different $\mathrm{V}(\mathrm{IV})$ and $\mathrm{V}(\mathrm{V})$ phosphates and related compounds is carried out. © 1988 Academic Press, Inc.


## Introduction

Vanadium phosphorus oxides are used as heterogeneous catalysts in various organic reactions, such as the mild oxidation of butenes (1) or butane (2) to maleic anhydride. The redox mechanism occurring during catalysis results from the ability of vanadium to exist in several oxidation states, and a variety of coordinations. This oxidation catalysis depends on the crystal structure of those mixed frameworks, and their structural analysis is very important in understanding the mechanism of the catalytic reaction. Moreover such mixed frameworks, involving $d^{n}$ transition ions are susceptible to present interesting physical properties. For this reason, the investigation of the sys-
$600^{\circ} \mathrm{C}$ in an platinum crucible in air in order to eliminate $\mathrm{CO}_{2}, \mathrm{NH}_{3}$, and $\mathrm{H}_{2} \mathrm{O}$. After cooling the amount of $\mathrm{V}_{2} \mathrm{O}_{3}$ or metallic vanadium required for the reduction of vanadium (V) into vanadium (IV) was added with the reaction product. The mixture was homogeneized by grinding and introduced into a platinum tube which was placed in an evacuated silica ampoule. The reaction mixture was heated for 5 days at $550^{\circ} \mathrm{C}$. After quenching at room temperature, a greenish slightly sintered powder was obtained.

Single crystal growth. Single crystals were grown in the following way: approximately 500 mg of $\beta-\mathrm{VOPO}_{4}$, prepared by conventional methods (4), was introduced in a platinum crucible containing traces of $\mathrm{K}_{2} \mathrm{O}$. Such traces were obtained by fusing $\mathrm{KHSO}_{4}$ in the platinum crucible, short leaching in hot water, and heating at $800^{\circ} \mathrm{C}$. The reaction mixture was placed in an evacuated silica ampoule and heated for 5 days at $550^{\circ} \mathrm{C}$. The crystals grew on the walls of the platinum tube in the form of green needles with a rectangular section.
$X$-ray analysis. The cell parameters were determined from the single crystal X-ray diffraction study. They allowed the X-ray powder diffraction pattern to be indexed correctly, except for very weak extra lines which correspond to the $\mathrm{V}(\mathrm{III})$ diphosphate $\mathrm{KVP}_{2} \mathrm{O}_{7}$ isotypic to $\mathrm{KMoP}_{2} \mathrm{O}_{7}$ (5). This is easily explained by the low stability of the oxide $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$. Further heating at $600^{\circ} \mathrm{C}$ led indeed to the formation of a great amount of $\mathrm{KVP}_{2} \mathrm{O}_{7}$.

## Structure: Determination and Refinement

Unit cell parameters were determined by least-squares refinement of the setting angles for 25 reflections [ $3^{\circ}<\theta(\operatorname{Mo} K \alpha)<17^{\circ}$ ] automatically centered on an Enraf-Nonius CAD-4 diffractometer. Intensity data were recorded on the same instrument with the experimental conditions given in Table I. The data were corrected for Lorentz and

TABLE I
Experimental Data

| Crystal form and size | $\begin{aligned} & \text { Green needle, } 0.024 \\ & \times 0.032 \times 0.312 \\ & \mathrm{~mm} \end{aligned}$ |
| :---: | :---: |
| $\theta_{\text {max }}$ | $45^{\circ}$ |
| Index range: $h$ | $0 \quad 23$ |
| $k$ | 019 |
| $l$ | 014 |
| Scan type | $\omega-\theta$ |
| Scan angle | $0.9+0.35 \tan \theta$ |
| Counter slit aperture | $1+\tan \theta$ |
| Monochromator | Graphite |
| Number of $h k l$ with $I \geq 3 \sigma(I)$ | 574 |
| Number of refined parameters | 104 |
| $R$ | 0.049 |
| $R_{\text {w }}$ | 0.055 |
| $\Delta / \sigma_{\text {max }}$ | 0.5 |
| $\delta \rho_{\text {max }}$ | $3 \mathrm{e}^{-} \AA^{-3}$ |

polarization effect but no absorption correction was applied. Scattering factors and anomalous dispersion were taken from the International Tables for X-ray Crystallography (6).

The structure determination was first carried out in the centrosymmetrical Pnam space group consistent with the observed systematic extinctions. The atomic coordinates of vanadium and potassium were deduced from the Patterson function. The remaining atoms were located by subsequent Fourier series. The refinement of the atomic coordinates and isotropic thermal factors was carried out by the full-matrix least-squares method and unit weights. This led to thermal factors often greater than $4 \AA^{2}$ which indicated that some atoms were shifted to some extent from a mirror plane ( $V(1)$ and $V(2)$ ) and the symmetry center (V(3)). As a consequence, the refinement was performed, in a second step, in the noncentrosymmetric space group $P n a 2_{1}$. Having raised the constraints for the atomic coordinates of vanadium, smaller values for the isotropic thermal parameters were obtained. However, nega-

TABLE II
Atomic Parameters

| Atom | $X$ | $Y$ | $Z$ | $B_{\text {iso }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $V(1)$ | 0.1005(2) | 0.6612(3) | $0.2500(0)$ | 0.57(6) |
| $V(2)$ | $0.1901(2)$ | 0.3392 (3) | 0.2692 (19) | $0.72(7)$ |
| $\mathrm{V}(3)$ | 0.0013(4) | $0.0017(6)$ | $0.0412(14)$ | 0.89(7) |
| K(1) | $0.1728(4)$ | $0.1371(6)$ | $0.7612(37)$ | 3.16(14) |
| K(2) | $0.3619(5)$ | $0.0352(7)$ | $0.2418(31)$ | $4.31(21)$ |
| $\mathrm{P}(1)$ | $0.3247(10)$ | $0.3886(15)$ | -0.0430(29) | 0.97(28) |
| $P(2)$ | $0.3285(10)$ | $0.3916(14)$ | -0.4435(32) | 0.97(27) |
| $\mathrm{P}(3)$ | $0.0297(8)$ | 0.2898(14) | $0.0511(26)$ | 0.67(21) |
| $\mathrm{P}(4)$ | 0.0258(8) | 0.2936 (14) | 0.4589(25) | 0.67(23) |
| $\mathrm{O}(1)$ | $0.1534(8)$ | $0.5488(13)$ | $0.2773(48)$ | 0.83(28) |
| O(2) | 0.1560 (14) | 0.7569(23) | $0.4344(40)$ | 1.03(49) |
| O(3) | $0.1436(14)$ | 0.7662(22) | 0.0641 (44) | 1.03(51) |
| O(4) | $0.0273(16)$ | $0.6255(25)$ | $0.4630(37)$ | 0.99 (44) |
| O(5) | $0.0177(16)$ | $0.6289(25)$ | $0.0933(37)$ | 0.99(51) |
| O (6) | $0.1093(19)$ | $0.3465(25)$ | 0.0540 (57) | $1.11(56)$ |
| O(7) | $0.1092(19)$ | $0.3299(25)$ | $0.4523(52)$ | 1.11(58) |
| $\mathrm{O}(8)$ | $0.2638(12)$ | $0.4137(20)$ | 0.4163(33) | 0.72 (39) |
| $\bigcirc(9)$ | 0.2216(10) | 0.2074(16) | 0.2410 (59) | 2.27(42) |
| O(10) | $0.2504(11)$ | 0.4086(19) | 0.0433(38) | 0.72(35) |
| O(11) | $0.0327(13)$ | $0.1702(24)$ | -0.0117(37) | 0.76(47) |
| O(12) | $0.0071(14)$ | $0.0095(20)$ | $0.2699(64)$ | 3.96 (56) |
| O(13) | -0.0181(13) | -0.1649(23) | $0.0486(45)$ | $0.76(38)$ |
| O(14) | -0.1101(14) | 0.0328(22) | $0.0604(40)$ | 1.38(40) |
| $\mathrm{O}(15)$ | $0.1112(14)$ | -0.0263(22) | $0.0309(43)$ | $1.38(45)$ |
| O(16) | -0.0078(8) | $0.2921(13)$ | 0.2483 (53) | $1.18(30)$ |
| O(17) | 0.3022(12) | 0.4297(19) | -0.237(12) | 3.87(47) |

tive correlations occurred between the $B$ values of independent atoms which were equivalent by a mirror plane in the centrosymmetrical Pnam space group. For the atomic pairs located on both sides of this pseudo-mirror plane in the $P n a 2_{1}$ group, it was observed during the structure refinement that if one of the two isotropic $B$ factors increased, the second one decreased and could be negative. To eliminate such an effect, subsequent refinement cycles were carried out using the average of their $B$ values obtained from the previous cycles from each of the correlated atoms. The thermal parameters were refined isotropically since anisotropic refinement allowed for only two reflections per parameter. The final stage of refinement led to $R=0.049, R_{w}=0.055$ and to the parameters of the Table II. ${ }^{1}$

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## Description of the Structure: Structural Relationships

The host lattice of this vanadophosphate (Figs. 1 and 2) is built up from corner-sharing $\mathrm{VO}_{6}$ octahedra, $\mathrm{VO}_{5}$ square pyramids, and disphosphate groups $\mathrm{P}_{2} \mathrm{O}_{7}$. This mixed framework delimits intersecting tunnels running along $b$ and $c$, where the potassium ions are located.

The three crystallographically independent vanadium atoms are in the +4 oxidation state. The atoms $V(1)$ exhibit a square pyramidal coordination. In those polyhedra the vanadium atoms are displaced from the basal plane formed by the oxygen atoms by $0.463,0.465$, and $0.082 \AA$ for $V(1), V(2)$, and V(3), respectively. Consequently, very short apical vanadium-oxygen bonds are observed: $1.585,1.606$, and $1.674 \AA$ for $(\mathrm{V}(1-\mathrm{O}(1), \mathrm{V}(2)-\mathrm{O}(9)$, and $\mathrm{V}(3)-\mathrm{O}(12)$, respectively (Table III). These short V-O distances can be interpreted as the result of


Fig. 1. Projection of the $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$ structure on to the $(\mathrm{ab})$ plane showing the pseudo-rectangular tunnels and the "snail-shell-shaped" tunnels running along $c$.
the ability of V(IV) to form a vanadyl ion $\mathrm{VO}^{2+}$, leading to the formulation of $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$. Such V-O bonds are indeed observed in several mixed frameworks containing V(IV): $1.59 \AA$ in VO $\mathrm{SiP}_{2} \mathrm{O}_{8}(7), \beta-\mathrm{VOSO}_{4}(8)$, and $\mathrm{VO}\left(\mathrm{PO}_{3}\right)_{2}(9)$, $1.62 \AA$ in $\alpha-$ VOSO $_{4}(10), 1.68 \AA$ in $\mathrm{VOMoO}_{4}$ (11), and ( VO$)_{2} \mathrm{P}_{2} \mathrm{O}_{7}$ (12). This ability of
$\mathrm{V}(\mathrm{IV})$ to form a short $\mathrm{V}=\mathrm{O}$ bond can be compared to that of $\mathrm{Mo}(\mathrm{V})$ which also exhibits a $d^{1}$ configuration. $\mathrm{MoPO}_{5}$ (13) and $\mathrm{K}_{4} \mathrm{Mo}_{8} \mathrm{P}_{12} \mathrm{O}_{52}$ (14) also show similar $\mathrm{MoO}_{6}$ octahedra characterized by a molybdenyl $\mathrm{Mo}=\mathrm{O}$ bond of $1.66 \AA$. Nevertheless, it is worth pointing out that the " $\mathrm{MO}_{6}$ " octahedra are almost regular in the $\mathrm{Mo}(\mathrm{V})$ oxides,


Fig. 2. Projection of the $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$ structure on to the ( $a \mathrm{c}$ ) plane showing the tunnels running along $c$.

TABLE III
Interatomic Distances ( $\AA$ ) and Bond Angles ( ${ }^{\circ}$ ) in the $\mathrm{V}(1) \mathrm{O}_{5}$, $\mathrm{V}(2) \mathrm{O}_{6}$, and $\mathrm{V}(3) \mathrm{O}_{6}$ Polyhedra

| V(1) | $\mathrm{O}(1)$ | $\mathrm{O}(2)$ |  | $\mathrm{O}(3)$ | $\mathrm{O}(4)$ | O(5) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O(1) | 1.59(2) | 2.63(3) |  | 2.92(4) | 2.72(4) | 2.87(3) |
| O(2) | 94(1) | 1.98(3) |  | 2.71(4) | 2.70 (4) | 3.76(4) |
| O(3) | 111(1) | 87(1) |  | 1.96(3) | 3.89(4) | 2.70 (4) |
| $\mathrm{O}(4)$ | 96(1) | 84(1) |  | 152(1) | 2.05(3) | 2.70(4) |
| O(5) | 111(1) | 154(1) |  | 89(1) | 87(1) | 1.88(3) |
| V(2) | $O(1)$ | O(6) | $\mathrm{O}(7)$ | $\mathrm{O}(8)$ | O(9) | $\mathrm{O}(10)$ |
| O(1) | 2.46(2) | 2.92(4) | 2.90(4) | 2.66(3) | 4.06(5) | 2.88(3) |
| O(6) | 79(1) | 2.11(4) | 2.91(6) | 3.85(4) | 2.86(4) | 2.56(4) |
| O(7) | 81(1) | 92(1) | 1.94(4) | 2.87(4) | 2.85(4) | 3.97(4) |
| $\mathrm{O}(8)$ | 74(1) | 150(1) | 97(1) | ) 1.88(2) | 2.77(3) | 2.73(4) |
| O(9) | 172(2) | 100(1) | 107(1) | 105(1) | 1.61(2) | 2.75(4) |
| O(10) | 78(1) | 75(1) | 157(1) | 86(1) | 94(1) | 2.11(3) |
| V(3) | O(11) | $\mathrm{O}(12)$ | $\mathrm{O}\left(12^{\mathrm{i}}\right)$ | $\mathrm{O}(13)$ | O(14) | $\mathrm{O}(15)$ |
| O(11) | 2.03(3) | 2.78(4) | 2.68(4) | 3.93(4) | 2.98(3) | 2.63(4) |
| O(12) | 97(1) | 1.67(5) | 3.66(4) | 2.59(5) | 2.56(4) | $2.55(5)$ |
| $\mathrm{O}\left(12^{\text {i }}\right.$ ) | 84(1) | 179(4) | 1.99(5) | ) $2.70(5)$ | 2.82(5) | 2.81(5) |
| O(13) | 169(1) | 92(1) | 87(1) | 1.92(3) | 2.76(4) | 2.75(4) |
| $\mathrm{O}(14)$ | 96(1) | 89(1) | 91(1) | 90(1) | 1.98(3) | 3.92(4) |
| $\mathrm{O}(15)$ | 83(1) | 89(1) | 91(1) | 91(1) | 178(1) | 1.94(3) |

Note. The diagonal indicates the M-O bond length $(\AA)$. The values above the diagonal are the $0 \ldots$ lengths $(\AA)$ and the values below are the $\mathrm{O}-\mathrm{M}-\mathrm{O}$ angles $\left({ }^{\circ}\right)$.
the molybdenum ion being off centered, whereas they are generally more distorted in the $\mathrm{V}(\mathrm{IV})$ oxides as shown here for $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$ (Table III). However, the $d^{1}$ electronic configuration cannot be considered as the only factor governing the existence of short $\mathrm{V}=\mathrm{O}$ bonds since a similar behavior is observed in various $\mathrm{V}(\mathrm{V})$ oxides. $\alpha-\mathrm{VPO}_{5}$ (15), $\beta-\mathrm{VPO}_{5}$ (16), and $\mathrm{VAsO}_{5}$ (17) have their $\mathrm{VO}_{6}$ octahedra characterized by similar short $\mathrm{V}=\mathrm{O}$ bonds of $1.58,1.59$, and $1.59 \AA$, respectively. The ability of $V(I V)$ and $V(V)$ to form a very short $\mathrm{V}=\mathrm{O}$ bond induces the formation of $\mathrm{VO}_{5}$ pyramids confirmed in $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$ by the existence of the $\mathrm{V}(1) \mathrm{O}_{5}$ square pyramid. The pyramidal coordination of vanadium
has indeed been observed up to the present only in mixed valence vanadium oxides $\mathrm{Cs}_{2} \mathrm{~V}_{5} \mathrm{O}_{13}$ (18) and $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{O}_{8}$ (19), in vanadium bronzes $A_{x} \mathrm{~V}_{2} \mathrm{O}_{5}$ (20) and $\mathrm{Li}_{1+x} \mathrm{~V}_{3} \mathrm{O}_{8}$ (21), and in the $\mathrm{V}(\mathrm{V})$ oxide $\mathrm{V}_{2} \mathrm{O}_{5}$ (22). The $\mathrm{V}(1)-\mathrm{O}(1)$ distance $(1.585 \AA$ ) observed in the pyramid $\mathrm{V}(1) \mathrm{O}_{5}$ is rather close to that observed in the other vanadium oxides whereas the V-O bonds of the basal plane $\langle\mathrm{V}-\mathrm{O}\rangle=1.97 \AA$ is close to those observed in $\mathrm{Cs}_{2} \mathrm{~V}_{5} \mathrm{O}_{13}(\langle\mathrm{~V}-\mathrm{O}\rangle=2.05 \AA), \mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{O}_{8}(\langle\mathrm{~V}-$ $\mathrm{O}\rangle=1.94 \AA$ ) in the vanadium bronzes ( $\langle\mathrm{V}-$ $\mathrm{O}\rangle=1.90 \AA$ ), and in $\mathrm{V}_{2} \mathrm{O}_{5}(\langle\mathrm{~V}-\mathrm{O}\rangle=1.89$ $\AA$ ). The smaller $\mathrm{V}-\mathrm{O}$ distances observed for the vanadium bronzes and $\mathrm{V}_{2} \mathrm{O}_{5}$ result from the increase of the $\mathrm{V}(\mathrm{V})$ character. Moreover it is worth pointing out that the

TABLE IV
Interatomic Distances ( $\AA$ ) and Bond Angles ( ${ }^{\circ}$ ) in The $\mathrm{PO}_{4}$ Tetrahedra

| $(1)$ | $O\left(2^{\text {iii }}\right)$ | $O(10)$ | $O\left(14^{\text {iii }}\right)$ | $O(17)$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{O}\left(2^{\text {ii }}\right)$ | $1.54(3)$ | $2.50(3)$ | $2.68(4)$ | $2.44(5)$ |
| $\mathrm{O}(10)$ | $113(2)$ | $1.46(3)$ | $2.52(3)$ | $2.25(8)$ |
| $\mathrm{O}\left(14^{\text {iii }}\right)$ | $115(2)$ | $109(1)$ | $1.63(3)$ | $2.69(8)$ |
| $\mathrm{O}(17)$ | $104(2)$ | $97(2)$ | $116(2)$ | $1.54(8)$ |
| $\mathrm{P}(2)$ | $\mathrm{O}\left(3^{\text {iii }}\right)$ | $\mathrm{O}\left(8^{\text {iv }}\right)$ | $\mathrm{O}(15 \mathrm{v})$ | $\mathrm{O}(17)$ |
| $\mathrm{O}\left(3^{\text {ii }}\right)$ | $1.50(3)$ | $2.56(3)$ | $2.43(4)$ | $2.54(6)$ |
| $\mathrm{O}\left(8^{\text {iv }}\right)$ | $115(2)$ | $1.54(3)$ | $2.43(3)$ | $2.62(9)$ |
| $\mathrm{O}\left(15^{v}\right)$ | $113(2)$ | $110(2)$ | $1.42(3)$ | $2.32(7)$ |
| $\mathrm{O}(17)$ | $108(2)$ | $111(2)$ | $99(2)$ | $1.63(8)$ |
| $\mathrm{P}(3)$ | $\mathrm{O}\left(4^{\text {vi }}\right)$ | $\mathrm{O}(6)$ | $\mathrm{O}(11)$ | $\mathrm{O}(16)$ |
| $\mathrm{O}\left(4^{\text {vi }}\right)$ | $1.52(3)$ | $2.49(4)$ | $2.55(4)$ | $2.31(4)$ |
| $\mathrm{O}(6)$ | $109(2)$ | $1.54(3)$ | $2.45(4)$ | $2.56(4)$ |
| $\mathrm{O}(11)$ | $119(2)$ | $112(2)$ | $1.43(3)$ | $2.45(4)$ |
| $\mathrm{O}(16)$ | $96(1)$ | $111(2)$ | $109(1)$ | $1.58(4)$ |
| $\mathrm{P}(4)$ | $\mathrm{O}\left(5^{\text {vii }}\right)$ | $\mathrm{O}(7)$ | $\mathrm{O}\left(13^{\text {viii }}\right)$ | $\mathrm{O}(16)$ |
| $\mathrm{O}\left(5^{\text {vii }}\right)$ | $1.52(3)$ | $2.48(4)$ | $2.44(4)$ | $2.68(5)$ |
| $\mathrm{O}(7)$ | $110(2)$ | $1.51(4)$ | $2.55(4)$ | $2.56(4)$ |
| $\mathrm{O}\left(13^{\text {viii }}\right)$ | $103(2)$ | $110(2)$ | $1.61(3)$ | $2.66(4)$ |
| $\mathrm{O}(16)$ | $116(1)$ | $108(2)$ | $110(1)$ | $1.64(4)$ |

Note. Symmetry code. i: $-x,-y, z-0.5$; ii: $0.5-$ $x, y-0.5, z-0.5$; iii: $0.5+x, 0.5-y, z$; iv: $x, y, z-$ 1; v: $0.5-x, 0.5+y, z-0.5$; vi: $-x, 1-y, z-0.5$; vii: $-x, 1-y, z+0.5$; viii: $-x,-y, z+0.5$; ix: $x, y, z$ $+1 ; \mathrm{x}: 0.5-x, y-0.5, z+0.5$.

coordination of vanadium in $\mathrm{V}_{2} \mathrm{O}_{5}$ and in the vanadium bronzes is in fact intermediate between a pyramid and an octahedron, so that their structure can also be described as the association of distorted octahedra (23).

The diphosphate groups exhibit an eclipsed configuration with $\mathrm{P}-\mathrm{O}$ distances and $\mathrm{O}-\mathrm{P}-\mathrm{O}$ bond angles (Table IV) close to those generally observed in diphosphate compounds and especially in diphosphate tungsten bronzes (24). In particular it can be seen that the $\mathrm{P}-\mathrm{O}$ distances corresponding to the bridging oxygen of $\mathrm{P}_{2} \mathrm{O}_{7}$ is higher than the other $\mathrm{P}-\mathrm{O}$ bonds in agreement with the Brown theory (25).

In $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$ the existence of [ $\mathrm{VO}_{5}$ ] chains of corner-sharing $\mathrm{VO}_{6}$ octahedra running along $c$ (Fig. 2) is characteristically common in several $V(V)$ and $V(I V)$ phosphates. Such isolated $\mathrm{ReO}_{3}$-type files are indeed observed in $\alpha-\mathrm{VPO}_{5}$ (Fig. 3a), $\mathrm{VP}_{2}$ $\mathrm{SiO}_{9}$ (Fig. 4a), and $\mathrm{VP}_{2} \mathrm{O}_{7}$ (Fig. 5). $\mathrm{V}_{2} \mathrm{P}_{2} \mathrm{O}_{9}$ also exhibits $\mathrm{ReO}_{3}$-type chains of $\mathrm{VO}_{6}$ octahedra (Fig. 6a), but contrary to the previous structures, the octahedral chains are not isolated: two $\mathrm{ReO}_{3}$-type chains share the edge of their octahedra (Fig. 6a), forming double $\mathrm{ReO}_{3}$-type files which are connected to each other through diphosphate groups (Fig. 6b). Infinite files of corner-sharing oc-


Fig. 3. The $\alpha-\mathrm{VPO}_{5}$ structure viewed: (a) along $a$ showing the $\mathrm{ReO}_{3}$-type files, (b) along $c$ showing the connection between the files.


Fig. 4. Partial projection of the $\mathrm{VP}_{2} \mathrm{SiO}_{9}$ structure viewed: (a) along a showing the $\mathrm{ReO}_{3}$-type files, (b) along $c$ showing the connection between the files.
tahedra are also observed in $\beta$ - $\mathrm{VPO}_{5}$ (Fig. 7), as for $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$. There chains are isolated from each other, but the $\mathrm{O}-\mathrm{O}-\mathrm{O}$ bond angle between two successive octahedra is close to $120^{\circ}$ (or $60^{\circ}$ ) instead of $90^{\circ}$ as in $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$. Such files can be described as hexagonal tungsten bronze (HTB) type files. The adaptability of the diphosphate groups to the $\mathrm{ReO}_{3}$-type files is a remarkable feature of the structure of $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$. Each $\mathrm{P}_{2} \mathrm{O}_{7}$ group shares two corners with


Fig. 5. The $\mathrm{ReO}_{3}$-type files in $\mathrm{VP}_{2} \mathrm{O}_{7}$ and their connection by infinite chains of $\left[\mathrm{PO}_{3}\right]_{\text {l }}$.
the $\mathrm{V}(3) \mathrm{O}_{6}$ octahedra, and each octahedron of the file shares the four corners of its basal plane, forming mixed chains $\left[\mathrm{V}_{2} \mathrm{P}_{8} \mathrm{O}_{30}\right]_{\infty}$ running along $c$ (Fig. 8). Such mixed chains can also be recognized in the structure of $\mathrm{V}_{2} \mathrm{P}_{2} \mathrm{O}_{9}$ (Fig. 9). However, the $\left[\mathrm{V}_{2} \mathrm{P}_{8} \mathrm{O}_{30}\right]_{0}$ chains do not exist as isolated files. Two such files are condensed by sharing the edges of the $\mathrm{VO}_{6}$ and simultaneous elimination of two disphosphate groups leading to infinite chains $\left[\mathrm{V}_{4} \mathrm{P}_{12} \mathrm{O}_{46}\right]_{\infty}$. This adaptability of the diphosphate groups to $\mathrm{ReO}_{3}-$ type files can be compared to that observed in the diphosphate tungsten bronzes $A_{x}$ $\left(\mathrm{P}_{2} \mathrm{O}_{4}\right)_{2}\left(\mathrm{WO}_{3}\right)_{2 m}$ described by Labbe et al. (26). The structure of those latter bronzes is indeed described as $\mathrm{ReO}_{3}$-type slabs connected through diphosphate planes. It is worth pointiag out that the presence of diphosphate groups linked to $\mathrm{ReO}_{3}$-type files is rather rare in the vanadophosphates. The analysis of the structure of $\mathrm{VP}_{2} \mathrm{O}_{7}$ shows that its $\mathrm{ReO}_{3}$-type files are connected through infinite chains $\left[\mathrm{PO}_{3}\right]_{\infty}$ of cornersharing $\mathrm{PO}_{4}$ tetrahedra (Fig. 5) whereas in the other vanadophosphates, the $\mathrm{ReO}_{3}$-type files are connected to each other through single $\mathrm{PO}_{4}$ tetrahedra. Moreover contrary


Fig. 6. $\mathrm{V}_{2} \mathrm{P}_{2} \mathrm{O}_{9}$ structure viewed: (a) along the $c$ axis, (b) along the $a$ axis.
to $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$ their structure is built up from mixed chains $\left[\mathrm{VPO}_{8}\right]_{\infty}$ in which one tetrahedron alternates with one octahedron (Fig. 9a). In $\alpha-\mathrm{VPO}_{5}$ and $\beta-\mathrm{VPO}_{5}$ such chains run along $a$ (Fig. 3a) and $b$ (Fig. 7a), respectively. In both compounds, each octahedron of a chain shares two opposite corners with one $\mathrm{PO}_{4}$ tetrahedron of the adjacent chain, but the relative orientation of the chains in $\alpha-\mathrm{VPO}_{5}$ (Fig. 9b) is different from the one in $\beta$ - $\mathrm{VPO}_{5}$ (Fig. 9c).

The result is that the two other corners of each octahedron which are shared with an-


Fig. 7. Projection of the $\beta-\mathrm{VPO}_{5}$ structure along $b$ showing the HTB-type chains running along $a$.
other $\mathrm{VO}_{6}$ octahedron of the adjacent chains form an $\mathrm{ReO}_{3}$-type chain parallel to $c$ in $\alpha$ - $\mathrm{VPO}_{5}$ (Fig. 3b) and a HTB-type chain parallel to $a$ in $\beta-\mathrm{VPO}_{5}$ (Fig. 7b). The structure of $\mathrm{V}_{2} \mathrm{P}_{2} \mathrm{O}_{9}$ is also built up from those mixed chains, which are associated in the (100) plane through the edges of their octahedra (Fig. 6b). Along $a$, the $\mathrm{PO}_{4}$ tetrahedra


Fig. 8. $\left[\mathrm{V}_{2} \mathrm{P}_{8} \mathrm{O}_{30}\right]_{\infty}$ chains running along $c$ in $\mathrm{K}_{2}(\mathrm{VO})_{3}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$.


FIG. 9. (a) $\left[\mathrm{VPO}_{8}\right]_{\infty}$ chain. Relative orientations of the $\left[\mathrm{VPO}_{8}\right]_{\alpha}$ chains in: (b) $\alpha-\mathrm{VPO}_{5}$, (c) $\beta-\mathrm{VPO}_{s}$.
of each chain share their corners forming the $\mathrm{P}_{2} \mathrm{O}_{7}$ groups, whereas the $\mathrm{VO}_{6}$ octahedra are also linked through their apices forming $\mathrm{ReO}_{3}$-type chains (Fig. 6a). The structure of $\mathrm{VSiP}_{2} \mathrm{O}_{9}$ also shows the mixed chain $\left[\mathrm{VPO}_{8}\right]_{\infty}$ formed from $\mathrm{VO}_{6}$ octahedra and $\mathrm{PO}_{4}$ tetrahedra running along the [110] direction (Fig. 4a), but in this case the orientations of the tetrahedron are different: two successive tetrahedra are in a trans position (Fig. 4b) while they are cis in the other oxides (Fig. 9a).

An interesting feature concerns the infinite $\mathrm{ReO}_{3}$-type or HTB-type $\left[\mathrm{VO}_{5}\right]_{\infty}$ file: in the same $\left[\mathrm{VO}_{5}\right]_{\infty}$ file, the vanadium ions are all displaced from the barycenter in the same direction, forming a row of dipoles similar to those observed in ferroelectric oxides. Moreover, it is worth pointing out that in all those compounds the neighboring rows of dipoles point in opposite directions, leading to an antiferroelectric-type configuration. In this respect $V(V)$, in spite of its $d^{\circ}$
configuration, differs from $\mathrm{Nb}(\mathrm{V})$ and $\mathrm{Ti}(\mathrm{IV})$ which exhibit several ferroelectric perovskites.

The host-lattice of $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$ is also interesting by its particular character of inter-secting-tunnel structure. The mixed chains [ $\left.\mathrm{V}_{2} \mathrm{P}_{8} \mathrm{O}_{30}\right]_{\infty}$ are linked to each other through [ $\mathrm{V}_{2} \mathrm{O}_{10}$ ] units formed from one $\mathrm{VO}_{5}$ pyramid and one $\mathrm{VO}_{6}$ octahedron sharing one corner (Fig. 1). This framework delimits two types of tunnels running along the $c$ axis, pseudorectangular tunnels similar to those observed in $\mathrm{P}_{8} \mathrm{~W}_{12} \mathrm{O}_{52}$ (27) and "snail-shellshaped" tunnels which resemble the pseudo-hexagonal tunnels observed in $\mathrm{Mo}_{5} \mathrm{O}_{14}$ (28).

Along the $b$ axis, the observed tunnel (Fig. 2) results from the superposition of pentagonal rings ( 3 octahedra +2 tetrahedra) and heptagonal rings ( 4 tetrahedra +2 octahedra +1 pyramid). The potassium ions K(1) belong to the "snail-shaped" tunnels whereas the cations $\mathrm{K}(2)$ are located at the intersection of the pseudo-rectangular tunnels and of the tunnels parallel to the $b$ axis.

TABLE V
Potassium-Oxygen
Distances ( $\AA$ )

| $\mathrm{K}(1)-\mathrm{O}\left(14^{\text {viii }}\right)$ | $=2.66(3)$ |
| :---: | :---: |
| $\mathrm{K}(1)-\mathrm{O}\left(15^{\mathrm{ix}}\right)$ | $=2.91$ (3) |
| $\mathrm{K}(1)-\mathrm{O}\left(11^{\mathrm{ix}}\right)$ | $=2.97(3)$ |
| $\mathrm{K}(1)-\mathrm{O}\left(8^{\mathrm{x}}\right)$ | $=2.99$ (3) |
| $\mathrm{K}(1)-\mathrm{O}\left(13^{\text {viii }}\right)$ | $=3.12(3)$ |
| $\mathrm{K}(1)-\mathrm{O}\left(1^{\mathrm{x}}\right)$ | $=3.19(2)$ |
| $\mathrm{K}(1)-\mathrm{O}\left(10^{\mathrm{x}}\right)$ | $=3.32(3)$ |
| $\mathrm{K}(1)-\mathrm{O}(7)$ | $=3.33$ (4) |
| $\mathrm{K}(2)-\mathrm{O}\left(4^{\text {ii) }}\right.$ ) | $=2.99$ (3) |
| $\mathrm{K}(2)-\mathrm{O}\left(16^{\text {iii) }}\right.$ ) | $=3.00(2)$ |
| $\mathrm{K}(2)-\mathrm{O}\left(17^{x}\right)$ | $=3.10(2)$ |
| $\mathrm{K}(2)-\mathrm{O}(9)$ | $=3.13(2)$ |
| $\mathrm{K}(2)-\mathrm{O}\left(6^{\mathrm{x}}\right)$ | $=3.17(4)$ |
| $\mathrm{K}(2)-\mathrm{O}\left(7^{\text {ii }}\right)$ | $=3.18(4)$ |
| $\mathrm{K}(2)-\mathrm{O}\left(10^{\mathrm{x}}\right)$ | $=3.28(3)$ |

Note. See symmetry code in Table IV.

To determine the maximum bond length of the potassium atom to oxygen, the Donnay and Allman (29) procedure with the revised "Ionic radii" of Shannon (30) was used $\mathrm{K}-\mathrm{O}_{\max }=3.35 \AA$. Accordingly each $K(1)$ ion can be considered to be surrounded by eight oxygen atoms with $\mathrm{K}-\mathrm{O}$ distances ranging from 2.66 to $3.33 \AA$ (Table V). The mean K-O distance ( $2.94 \AA$ ) is a little greater than that deduced from the ionic radii ( $2.91 \AA$ ) of Shannon (30). Most striking is the $\mathrm{K}(2)-\mathrm{O}$ bond lengths (Table V) which are all larger than $2.99 \AA$. The mean value of $3.12 \AA$ is much greater than the sum of the ionic radii ( $2.86 \AA$ ). Such behavior suggests a possible mobility of the K ions which could account for their rather high isotropic thermal parameter ( $B>3$ $\AA^{2}$ ). Thus, ion exchange properties of $\mathrm{K}_{2} \mathrm{~V}_{3} \mathrm{P}_{4} \mathrm{O}_{17}$ should be investigated.

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[^0]:    ${ }^{1}$ Lists of structure factors are available on request from the authors.

